

## A Juicy Dilemma

Project # 1 Mat 101

The juice division of Florence-Darlington Foods, Inc. blends cranberry juice with apple juice in 500 gallon vats prior to bottling. The resulting blend is advertised to be 42% cranberry juice. A new supervisor accidentally blended a 500 gallon vat that was 24% cranberry juice. Rather than discard the entire 500 gallons, the supervisor decides to correct the problem by draining off some of the 24% blend and adding pure cranberry juice to strengthen the blend to 42%. Making sure to end up with 500 gallons, how much of the 24% blend should the supervisor drain and replace with pure cranberry juice to correct the mistake? *Round all answers to the nearest tenth of a gallon or nearest tenth of a percent if needed.*

1. 120 gallons of the 24% blend are cranberry juice, and 380 gallons are apple juice.

210 gallons of the 42% blend are cranberry juice and 290 gallons are apple juice.

2. Suppose we drain 50 gallons of the 24% blend and replace it with pure cranberry juice. Use the table below to determine the resulting percentage of cranberry juice in the blend.

description	total volume	% cranberry juice	volume of cranberry juice
Starting mixture (gallons)	500	24%	120
Drain 50 gallons of blend	-50	24%	-12
Add 50 gallons of cranberry juice	50	100%	50
Resulting blend	<u>500</u>	<u>31.6%</u>	<u>158</u>

3. Redo the above table showing the results of draining 100 gallons of blend from the original 24% blend and replacing with pure cranberry juice.

description	total volume	% cranberry juice	volume of cranberry juice
Starting mixture (gallons)	500	24%	120
Drain 100 gallons of blend	<u>-100</u>	<u>24%</u>	<u>-24</u>
Add 100 gallons of cranberry juice	<u>+100</u>	<u>100%</u>	<u>100</u>
Resulting blend	<u>500</u>	<u>39.2%</u>	<u>196</u>

4. Redo the above table to show the draining of  $x$  gallons of blend from the original 24% blend and replacing with pure cranberry juice to achieve a 42% blend.

description	total volume	% cranberry juice	volume of cranberry juice
Starting mixture (gallons)	500	24%	120
Drain $x$ gallons of blend	$-x$	24%	$-0.24x$
Add $x$ gallons of cranberry juice	$x$	100%	$+x$
Resulting blend	500	42%	<u><math>120 + 0.76x</math></u>

5. What does the variable  $x$  represent?

- The percent of cranberry juice in the blend.
- The volume of cranberry juice in the original blend.
- The volume of cranberry juice in the final blend.
- The volume of juice to be drained and replaced with pure cranberry juice.

D

] ADD  
OR  
 $120 - 0.24x + x$

6. Why are the volumes in the second row negative?

- Because they were not apple juice.
- Because gravity acts downward.
- Because they are being removed from the blend.
- Because the percentage of cranberry juice is too low.

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7. In the table in # 4, why is the coefficient of  $x$  in the 3<sup>rd</sup> row positive 1?

- You are replacing the drained juice with 1 gallon of cranberry juice at a time.
- You are adding pure (100%) cranberry juice.
- You are only adding one type of juice.

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8. Use the last column of the table in # 4 to write a cranberry juice equation to solve for  $x$ . Your equation should show: **Starting amount - amount drained + amount added = desired amount**

- $500 - 24 + x = 42$
- $500 - 24x + 100x = 42$
- $120 - 0.24x + x = 0.42$
- $0.24(500) - 0.24x + x = 0.42(500)$

D

9. Solve your equation from # 8 for  $x$ .  $x = \underline{118.42}$ . This means that the supervisor should drain and replace 118.42 gallons of blend with pure cranberry juice.

## PART 1

$$24\% \text{ of } 500 = 120 \text{ cranberry } \left( \frac{24}{100} \times 500 \right)$$

remaining 380 = apple

$$42\% \text{ of } 500 = 210 \text{ cranberry } \left( \frac{42}{100} \times 500 \right)$$

remaining 290 = apple

## PART 8

$$\frac{120 + .76x}{500} = .42$$

$$120 + .76x = .42(500)$$