

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Find the values of  $x$  that satisfy the inequality  $0 \leq x + 7 \leq 12$ .

Answer: \_\_\_\_\_

2. Rationalize the denominator of the expression  $\sqrt{\frac{5x}{3y}}$ .

Answer: \_\_\_\_\_

3. Solve the following equation  $2x^2 - 3x - 9 = 0$ .

Answer: \_\_\_\_\_

4. Use the quadratic formula to solve  $2x^2 - 5x - 4 = 0$ .

Answer: \_\_\_\_\_

5. Simplify the expression  $\frac{4x^2 + 16x + 15}{6x^2 + 9x}$ .

Answer: \_\_\_\_\_

6. Find an equation of the line (slope-intercept form) that passes through the points  $(4,-1)$  and  $(-2,4)$ .

Answer: \_\_\_\_\_

7. Determine the domain of the function  $f(x) = \frac{x}{3x-5}$ .

Answer: \_\_\_\_\_

8. Let  $f(x) = 3\sqrt{2x+1}$  and  $g(x) = x^2 - 2$ . Find the rule for the composite function  $f \circ g$ .

Answer: \_\_\_\_\_

9. Find the value of  $\lim_{x \rightarrow -2} \frac{x+8}{x-1}$ .

Answer: \_\_\_\_\_

10. Find the value of  $\lim_{x \rightarrow 0} \frac{x^2 + 6x}{x}$ , if it exists.

Answer: \_\_\_\_\_

11. Find the value of  $\lim_{x \rightarrow 3^-} \frac{4-x}{x+3}$ , if it exists.

Answer: \_\_\_\_\_

12. A ball is thrown straight up into the air so that its height in feet after  $t$  seconds is given by  $s(t) = 128t - 16t^2$ .

a. Find the average velocity of the ball during the time interval  $[3, 3.1]$ .

Answer: \_\_\_\_\_

b. Find the instantaneous velocity of the ball at  $t = 3$  seconds.

Answer: \_\_\_\_\_

13. Let  $f(x) = \frac{1}{2}x^2 + 3x$ .

a. Find the slope of the tangent line to the graph of  $y = f(x)$  at  $x = 2$ .

Answer: \_\_\_\_\_

b. Find the equation of the tangent line to the graph of  $y = f(x)$  at  $x = 2$ .

Answer: \_\_\_\_\_

14. Find the derivative of the function  $f(x) = \frac{1}{8}x + 1$ .

Answer: \_\_\_\_\_

15. Find the derivative of the function  $f(x) = \sqrt{x} - \frac{1}{x}$ .

Answer: \_\_\_\_\_

16. Find the derivative of the function  $f(x) = \frac{4x^3}{x^2 + 1}$ .

Answer: \_\_\_\_\_

17. Find the derivative of the function  $f(x) = \sqrt{x^2 - 4x}$ .

Answer: \_\_\_\_\_

18. Let  $f(x) = \frac{1}{4}(x^2 + 2)(2x + 3)$ . Find the point(s) on the graph of  $f$  where the slope of the tangent line is equal to 10.

Answer: \_\_\_\_\_

19. Find  $\frac{dy}{du}$ ,  $\frac{du}{dx}$ , and  $\frac{dy}{dx}$  if  $y = u^{-5/3}$  and  $u = x^3 - 2x + 1$ .

Answer: \_\_\_\_\_

20. Find  $F'(3)$  if  $F(x) = f(g(x))$  and  $f(3) = 2$ ,  $f'(3) = 5$ ,  $f'(4) = 6$ ,  $g(3) = 4$ , and  $g'(3) = -2$ .

Answer: \_\_\_\_\_

21. Find the differential of the function  $f(x) = \frac{3}{x-1}$ .

Answer: \_\_\_\_\_

22. Find the interval(s) where  $f(x) = x^3 + \frac{9}{2}x^2 + 6x - 3$  is increasing and the interval(s) where it is decreasing.

Increasing: \_\_\_\_\_ Decreasing: \_\_\_\_\_

23. Find the relative maxima and minima, if any, of  $g(x) = 4x - x^4$ .

Maxima: \_\_\_\_\_ Minima: \_\_\_\_\_

24. Find the relative maxima and minima, if any, of  $h(t) = t^{1/3} - 3t$ .

Maxima: \_\_\_\_\_

Minima: \_\_\_\_\_

For problems 25-27, let  $f(x) = \sqrt[3]{x+1}$ .

25. Find the interval(s) where  $f(x)$  is concave upward.

Answer: \_\_\_\_\_

26. Find the interval(s) where  $f(x)$  is concave downward.

Answer: \_\_\_\_\_

27. Find the x-coordinate(s) of any point(s) of inflection.

Answer: \_\_\_\_\_

28. Find the horizontal and vertical asymptotes of the graph of  $y = \frac{x^2 + 2x + 1}{x^2 - 6x + 8}$ .

Horizontal: \_\_\_\_\_

Vertical: \_\_\_\_\_

29. Find the absolute maximum and the absolute minimum of  $f(x) = x^3 - 3x + 2$  on  $[-2, 4]$ .

Maximum: \_\_\_\_\_ Minimum: \_\_\_\_\_

30. A landlord owns an apartment building. When the rent for each apartment is \$700 per month, all 100 apartments are rented. The landlord estimates that each \$100 increase in the monthly rent will result in 10 apartments becoming vacant with no chance of being rented. What monthly rent amount will maximize the total monthly revenue?

Answer: \_\_\_\_\_